

The aim of Least Square Fitting is to find a set of parameters \vec{P} which minimize the quantity

$$\chi^2 = \sum \omega_i [X_i - x(f_i; \vec{P})]^2$$

called the "chi-square".

1. Selection of Data Sequence

A. For "Z: Real & Imag" Data Sequence:

$$X_i = \{ Z_r[0], Z_r[1], Z_r[2], \dots Z_r[Ns-1], Z_i[0], Z_i[1], \dots Z_i[Ns-1] \}$$

B. For "Z: Real" Data Sequence:

$$X_i = \{ Z_r[0], Z_r[1], Z_r[2], \dots Z_r[Ns-1] \}$$

C. For "Z: Mag & Phase" Data Sequence:

$$X_i = \{ |Z[0]|, |Z[1]|, |Z[2]|, \dots |Z[Ns-1]|, \phi[0], \phi[1], \dots \phi[Ns-1] \}$$

D. For "Y: Real & Imag" Data Sequence:

$$X_i = \{ Y_r[0], Y_r[1], Y_r[2], \dots Y_r[Ns-1], Y_i[0], Y_i[1], \dots Y_i[Ns-1] \}$$

E. and so on

2. Selection of Weighting Factor $\omega_i = 1/\sigma_i^2$ is calculated from the uncertainty (σ_i) of the i-th data point..

A. "Unity" : no weighting.

$$\sigma_i = 1$$

B. "Proportional" : the uncertainty of the real component of the data is proportional to its magnitude, and the uncertainty of the imaginary component is proportional to its magnitude

$$\sigma_i = \{ Z_r[0], Z_r[1], \dots Z_r[Ns-1], Z_i[0], Z_i[1], \dots, Z_i[Ns-1] \} \text{ for "Z: Real \& Imag"}$$

$$\sigma_i = \{ Z_r[0], Z_r[1], \dots Z_r[Ns-1] \} \text{ for "Z: Real"}$$

$$\sigma_i = \{ Z_r[0], Z_r[1], \dots Z_r[Ns-1], Z_i[0], Z_i[1], \dots, Z_i[Ns-1] \} \text{ for "Z: Mag \& Phase"}$$

$$\sigma_i = \{ Y_r[0], Y_r[1], \dots Y_r[Ns-1], Y_i[0], Y_i[1], \dots, Y_i[Ns-1] \} \text{ for "Y: Real \& Imag" }^{*1}$$

and so on...

C. "Modulus to Data" : the uncertainty of the each data is proportional to its modulus.

$$\sigma_i = \{ |Z[0]|, |Z[1]|, \dots |Z[Ns-1]|, |Z[0]|, |Z[1]|, \dots, |Z[Ns-1]| \} \text{ for "Z: Real \& Imag"}$$

$$\sigma_i = \{ |Z[0]|, |Z[1]|, \dots |Z[Ns-1]| \} \text{ for "Z: Real"}$$

$$\sigma_i = \{ |Z[0]|, |Z[1]|, \dots |Z[Ns-1]|, |Z[0]|, |Z[1]|, \dots, |Z[Ns-1]| \} \text{ for "Z: Mag \& Phase"}$$

$$\sigma_i = \{ |Y[0]|, |Y[1]|, \dots |Y[Ns-1]|, |Y[0]|, |Y[1]|, \dots, |Y[Ns-1]| \} \text{ for "Y: Real \& Imag" }^{*1}$$

and so on...

**1 I have designed the ZMAN according to a rule that bigger Z, bigger uncertainty. However, please note that this is not valid for Y, E data sequence in current ZMAN version.*